## McGraw-Hill Education

## MathLinks 9

## PATHWAYS TO SUCCESS

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## A Tour of Your Textbook

## Chapter Opener

Each chapter begins with a two-page spread that introduces you to the Big Idea and explores how the math covered in the chapter is used in real life. The Inquire and Explore feature provides inquiry questions related to the Big Idea for you to think about as you learn the content in the chapter.


## Get Ready

These two pages provide an overview of the prerequisite skills you will need to be successful in the chapter. Teaching boxes review content before you apply what you know.


## Three-Part Lesson Plan



The Know-Do-Understand icon emphasizes the BC curriculum model and divides the lesson into three parts.


Curricular competency icons are used in the Explore and Analyze and Connect and Reflect sections to show you which competencies you will need to use to solve a problem or answer a question. The icons are placed beside questions that are particularly good examples of those competencies.


## Explore and Analyze

These activities provide you with opportunities to investigate the content and build your own understanding of a new concept. On CONNECTschool, you will find links to websites, videos, worksheets, and other tools to provide support as you complete these activities. Many of the Explore and Analyze activities also promote inquiry-type problem solving and thinking.

## Develop Understanding

This section includes Examples and worked Solutions that show you how to use your prior knowledge and what you have learned in the Explore and Analyze activity to develop further understanding of the content.

- Thought bubbles prompt you to think about what you know and how you know it.
- Sometimes different methods of solving the same problem are shown. One way may make more sense to you than another.
- Calculator key-press sequences are shown where appropriate.
- The Show You Know section after each Example allows you to check that you understand the skill covered in the Example before moving on to the next.

- CONNECTschool provides videos, interactive activities, and links to websites for more information.


## Connect and Reflect

This section includes the Key Ideas and the Practise, Apply, and Extend questions. You will show what you have learned by practising, connecting, and reflecting on the concepts. Curricular competency icons indicate which competencies are addressed by selected key questions throughout the exercise set. Competency Check questions allow you to demonstrate your level of understanding of the concepts using multiple competencies.


## Other Features

## Tasks

The Tasks at the beginning of the book require you to use skills from more than one section or chapter. To promote an inquiry approach, you may need to do some research and explore some new concepts to complete the Task. You will apply what you learn to real life and create a presentation. CONNECTschool provides links to websites, worksheets, and helpful information to help you complete each Task. It also includes Project versions of each Task for students who prefer a more open inquiry-based approach to learning.


## Rich Problems

These questions, at the end of each chapter, require you to connect and apply various concepts in a challenging and engaging environment. You may wish to work individually or in small groups to complete them.

## Chapter Review

At the end of each chapter there is a Chapter Review. You can use the learning goals summary to self-assess your understanding of the chapter content. Also, review the Inquire and Explore questions to make sure you understand the Big Ideas from the chapter. The review is organized by section number so you can look back if you need help with a question. The Connect the
 Concepts section includes questions that use content from more than one section in the chapter.


## Answers

Answers are provided for all Practise, Apply, and Extend questions, except the Competency Check questions. Your teacher may use these to assess your understanding and progress. There are also answers for the Rich Problems and Chapter Review questions.

## Inquiry-Based Learning

## Why Should You Do Inquiry?

## Inquiry-based learning

- lets you to take control of your learning and build your own understanding
- allows you to develop meaningful questions that have multiple answers
- is an active exploration of a topic
- improves your logical reasoning, research, analysis, and communication skills
- offers opportunities to collaborate
- allows you to make connections between Big Ideas, concepts, and competencies


## Focus

- Ask questions about a topic that interests you.
- Use your existing knowledge and experiences to make conjectures and predictions about what the answer could be.
- Develop a plan for inquiry (research, using manipulatives, diagrams, technology, etc.).


## Evaluate

- Assess the inquiry process and your inquiry plan. What would you do differently next time?
- Are there some new inquiry questions that you would like to explore further?


## Share

- Use mathematical language and tools to tell what you learned. Explain how your inquiry question, findings, and solution are related. Why are your findings important?
- Describe how you can apply what you learned to new contexts.
- Reflect on your learning process.

The Inquiry Process

## Explore

- Implement your inquiry plan.
- Evaluate the information you learn.
- Connect what you learned to what you already knew.
- Share what you learned to help you generate more questions or revise your original question or prediction.
- Revise your inquiry plan if you need to.


## Analyze

- Organize the information you learned.
- Use what you learned to answer your inquiry question. You may also be able to draw further conclusions.
- Decide if the original predictions you made were correct. Explain your reasoning and prove your answer.
- Decide how you will present what you learned. What is the best way to show the math?


## Good Inquiry Questions and Responses

Inquiry works best when the question you start with meets the following criteria:

- The topic of the question is relevant and interesting to you.
- The question is open-ended. This means it cannot be answered with a simple yes or no.
- You will learn something new by responding to the question. If you already know the answer to an inquiry question, there is little point in investigating it.


## A Sample Inquiry

| Stage of Inquiry | Example |
| :---: | :---: |
| Focus <br> Your teacher tells you to imagine that you are in charge of renovating a two-storey office building where 200 people work. It already has several stairwells and one elevator, but the owners want to get more people to the second floor more easily. You are given a floor plan that shows the amount of space available to solve the problem. You need to choose a method of moving people between floors and draw it on the scale diagram. | After some thought, I decided to research <br> - the amount of space needed for an elevator and an escalator <br> - the dimensions of each <br> - the number of people each one can transport in the same amount of time <br> -the speed at which they can move people <br> - the difference in cost |
| Explore <br> Your teacher now asks you to start implementing your inquiry plan. | Using the Internet, I found the dimensions of a typical escalator and elevator and realized that either one would fit in the space allowed, although the escalator took up more room. There was not enough room on the diagram to include two elevators because of the layout of the available space. I discovered that an escalator can move more people more quickly. However, an escalator is more expensive to install. |
| Analyze <br> Next, you use the information you learned to draw conclusions to answer your inquiry question. You decide how you will share your conclusions with your class. | To present my findings, I drew my scale diagram of the escalator on the floor plan, showing my scale factor calculations. I made a table to compare the information for the escalator and elevator. I also created two graphs to show the difference in the time it would take for people to get to the second floor and the difference in cost. I concluded that the escalator is a better choice because it is so much faster. |
| Share <br> Present your findings to the class. Explain why you wanted to figure out the answer to the inquiry question and why it is an important question. Talk about where you might be able to use the skills or information you have learned in the future. | I wanted to compare escalators and elevators because I was curious about why you might choose one over the other. I learned that escalators move more people more quickly, but they are more expensive and take up more horizontal space than elevators; in some situations they might not be a practical choice. Learning how to compare different options in order to make a decision is a skill I might use when making big decisions in the future, like choosing what to do after high school, or what car to buy. |
| Evaluate <br> How well did your inquiry process work? Could you have done it differently to be more efficient? Did the process make you think of any other questions that you would like answered? | I wondered whether it would have been better to fit two elevators in the space by moving some walls. I also wondered how much office space would be lost by installing the escalator, which takes up more floor space. How important would that be? During my research, I noticed that the maintenance contracts for escalators are often much more expensive than for elevators. I did not take that into consideration for this project, but I wonder if that would change some people's choice. |

